



## M5-02: Bernoulli & Binomial Distributions

Part of the "Polling, Confidence Intervals, and the Normal Distribution" Learning Badge

Video Walkthrough: <https://discovery.cs.illinois.edu/m5-02/>

### Mathematics of Binary Events: Bernoulli & Binomial Distributions

#### Puzzle #1: A Fair Coin Flip

Suppose we flip a fair-sided coin and count how many heads we get. What are the possible outcomes?

<b>Outcome #1:</b>		<b>Probability Histogram for flipping a fair coin and counting the number of heads:</b> 
<b>P(Outcome #1):</b>		
<b>Outcome #2:</b>		
<b>P(Outcome #2):</b>		

#### Puzzle #2: A Dice Roll

Suppose we roll a fair, six-sided die and want to know if the result was 1.

<b>Outcome #1:</b>		<b>Probability Histogram for rolling a die and getting a 1:</b> 
<b>P(Outcome #1):</b>		
<b>Outcome #2:</b>		
<b>P(Outcome #2):</b>		

### Bernoulli Distribution for Discrete Random Variables

Any event that has exactly two outcomes with a fixed probability is called a Bernoulli distribution. Every Bernoulli distribution has a probability,  $p$ , describing the probability of that event occurring. *We know a lot of these already!*

<b>Event</b>	<b>Probability Distribution</b>
<b>Probability of drawing a queen in a deck of 52 cards.</b>	<b>Bernoulli(<math>p=1/13</math>)</b>
<b>Probability of "heads" on a fair coin.</b>	
<b>Probability of a 1 on a six-sided fair die.</b>	